

# Применение сетей Колмогорова-Арнольда для решения задач компьютерного зрения

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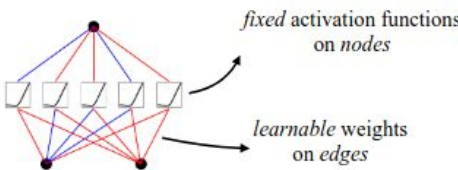
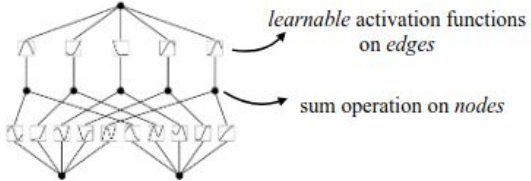
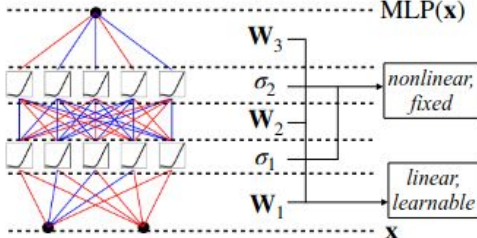
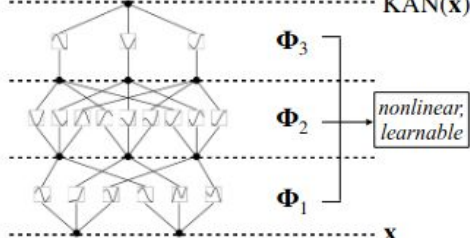


# План доклада

- 1) Обзор KAN
- 2) Литобзор
- 3) Направление исследования
- 4) Текущие результаты
- 5) Дальнейшее исследование

# Обзор KAN

# Основная идея KAN

Model	Multi-Layer Perceptron (MLP)	Kolmogorov-Arnold Network (KAN)
Theorem	Universal Approximation Theorem	Kolmogorov-Arnold Representation Theorem
Formula (Shallow)	$f(\mathbf{x}) \approx \sum_{i=1}^{N(\epsilon)} a_i \sigma(\mathbf{w}_i \cdot \mathbf{x} + b_i)$	$f(\mathbf{x}) = \sum_{q=1}^{2n+1} \Phi_q \left( \sum_{p=1}^n \phi_{q,p}(x_p) \right)$
Model (Shallow)	<p>(a)</p>  <p><i>fixed</i> activation functions on nodes</p> <p><i>learnable</i> weights on edges</p>	<p>(b)</p>  <p><i>learnable</i> activation functions on edges</p> <p>sum operation on nodes</p>
Formula (Deep)	$\text{MLP}(\mathbf{x}) = (\mathbf{W}_3 \circ \sigma_2 \circ \mathbf{W}_2 \circ \sigma_1 \circ \mathbf{W}_1)(\mathbf{x})$	$\text{KAN}(\mathbf{x}) = (\Phi_3 \circ \Phi_2 \circ \Phi_1)(\mathbf{x})$
Model (Deep)	<p>(c)</p>  <p><math>\mathbf{W}_3</math></p> <p><math>\sigma_2</math></p> <p><math>\mathbf{W}_2</math></p> <p><math>\sigma_1</math></p> <p><math>\mathbf{W}_1</math></p> <p><math>\mathbf{x}</math></p> <p>nonlinear, fixed</p> <p>linear, learnable</p>	<p>(d)</p>  <p><math>\Phi_3</math></p> <p><math>\Phi_2</math></p> <p><math>\Phi_1</math></p> <p><math>\mathbf{x}</math></p> <p>nonlinear, learnable</p>

# KAN vs MLP

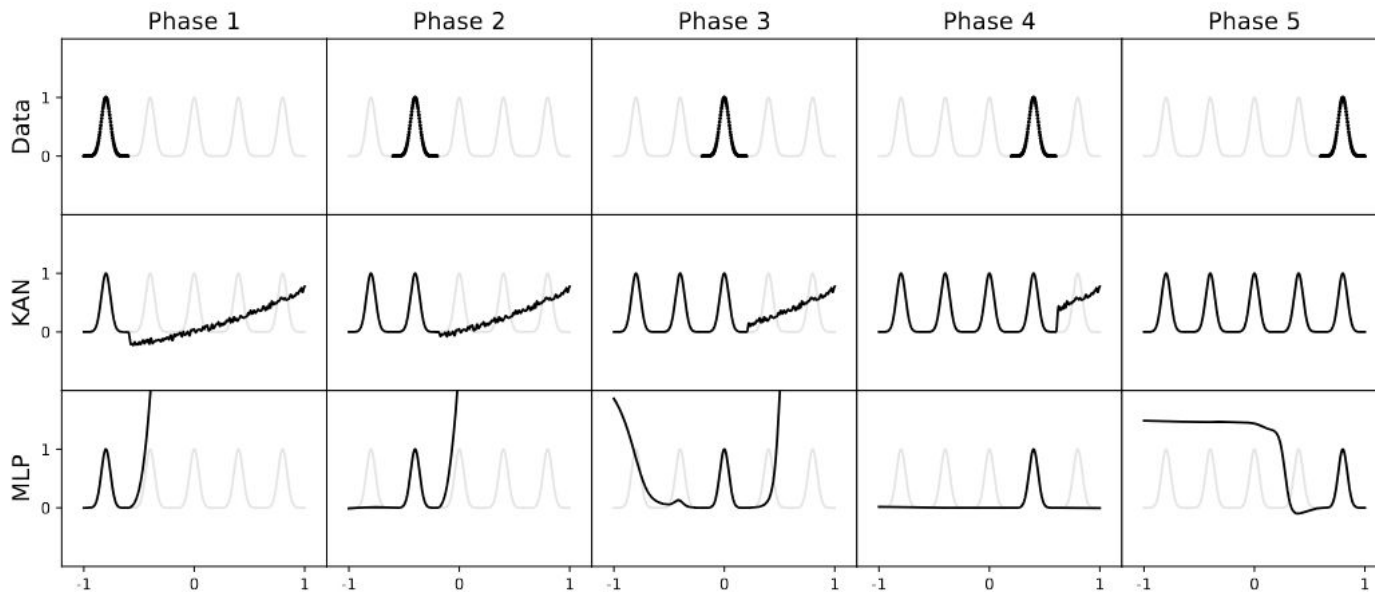


Figure 3.4: A toy continual learning problem. The dataset is a 1D regression task with 5 Gaussian peaks (top row). Data around each peak is presented sequentially (instead of all at once) to KANs and MLPs. KANs (middle row) can perfectly avoid catastrophic forgetting, while MLPs (bottom row) display severe catastrophic forgetting.

# KAN в задачах computer vision

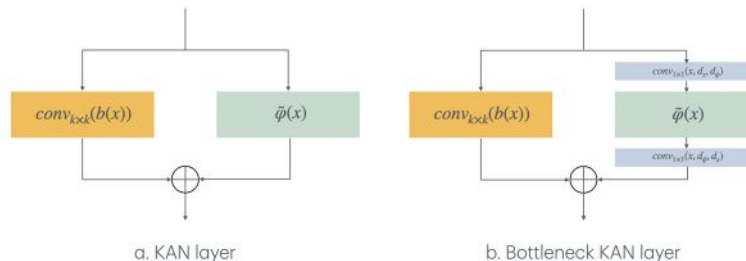


Figure 1: KAN Convolution (left) and Bottleneck KAN Convolution (right). The main difference between these two types of layers is an encoder-decoder convolutional layers on the right data stream.



Figure 2: Bottleneck Kolmogorov-Arnold Convolutional Mixture of Experts. The router and experts are placed between bottleneck convolutions, and each expert is a  $\tilde{\varphi}$  set of univariate functions. We use sparsely-gated mixture-of-experts [15].

Figure 3: Possible dropout layer placement inside KAGN Convolution layer: Full - before the layer, Poly - before computing Gram basis, and Degree - before weighted sum of previously computed basis.

# Литобзор

[https://docs.google.com/document/d/1BmdW4PVTmEM5WA25ypgqXOwJL\\_42EFL2BYIEtCww5f4/edit?tab=t.0](https://docs.google.com/document/d/1BmdW4PVTmEM5WA25ypgqXOwJL_42EFL2BYIEtCww5f4/edit?tab=t.0)

# Направление исследования



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# KOLMOGOROV-ARNOLD CONVOLUTIONS: DESIGN PRINCIPLES AND EMPIRICAL STUDIES

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A PREPRINT

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# KAN not Work: Investigating the Applicability of Kolmogorov-Arnold Networks in Computer Vision

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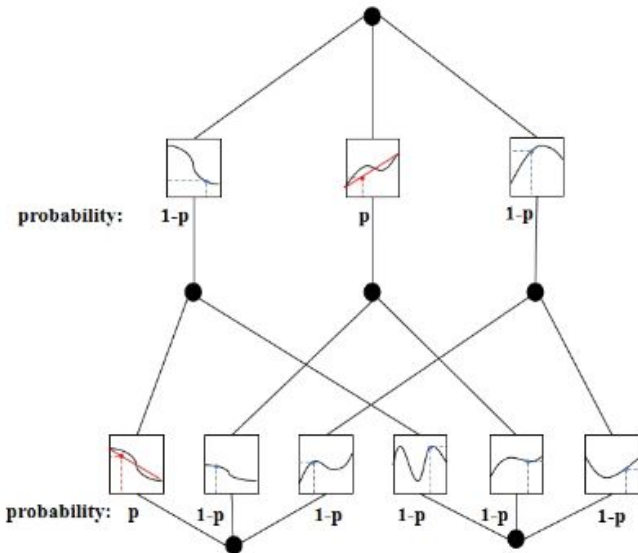


Table 2. **Experimental Model Configurations.** The baseline model (CNN+MLP) serves as a control for comparison with the CKAN and KAN-modified models.

Model	20%	40%	60%	80%	100%
CNN+MLP	62.31%	67.26%	69.93%	71.33%	71.96%
CKAN+CNN+MLP	61.82%	67.05%	69.03%	70.91%	71.88%
CNN+KAN	64.02%	68.15%	70.41%	72.13%	72.58%

Table 3. **Performance of Different Models on CIFAR-10 with Varying Dataset Sizes.** Each column shows the accuracy (%) of each model as the dataset size increases from 20% to 100%.

Model	10%	20%	30%	40%	50%
CNN+MLP	69.13%	67.93%	65.38%	63.88%	62.87%
CKAN+CNN+MLP	69.59%	66.73%	64.19%	62.56%	58.43%
CNN+KAN	69.95%	67.81%	64.33%	62.84%	59.20%

Table 4. **Performance of Different Models with Increasing Label Noise.** Each column represents the accuracy (%) as the label noise increases from 10% to 50%.

# U-Net-bin: hacking the document image binarization contest

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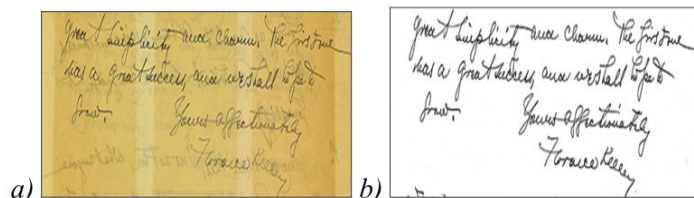


Fig. 1. Sample of document binarization application:  
(a) source image, (b) binarization result

Brief	Score	FM	Fps	PSNR	DRD
1) U-Net (Proposed method)	309	91.01	92.86	18.28	3.40
2) FCN (VGGNet)	455	89.67	91.03	17.58	4.35
3) Ensemble (3 DSN)	481	89.42	91.52	17.61	3.56
4) Ensemble (5 FCN, no postprocessing)	529	86.05	90.25	17.53	4.52
5) Ensemble (FCN, with postprocessing)	566	83.76	90.35	17.07	4.33
6) FCN	608	88.37	89.59	17.10	4.94
7) Howe based	635	89.17	89.88	17.85	5.66
Otsu	-	77.73	77.89	13.85	15.5
Sauvola	-	77.11	84.10	14.25	8.85

# U-KAN Makes Strong Backbone for Medical Image Segmentation and Generation

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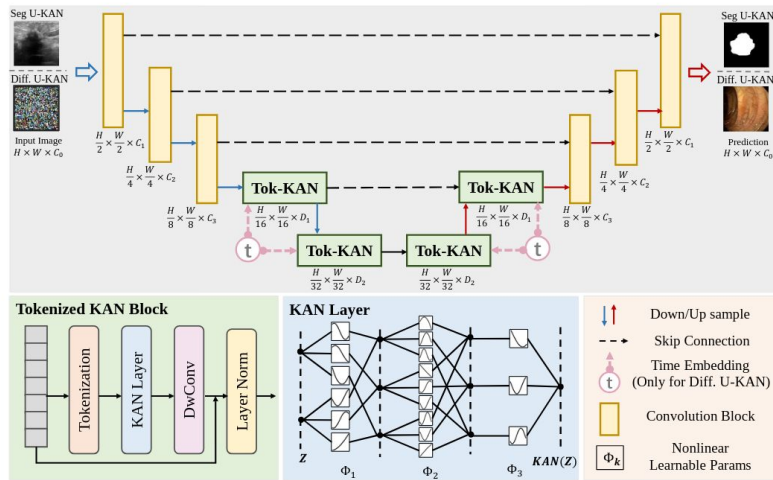


Figure 1: Overview of U-KAN pipeline. After feature extraction by several convolution blocks in Convolution Phrase, the intermediate maps are tokenized and processed by stacked Tok-KAN blocks in Tokenized KAN Phrase. The time embedding is only injected into the KAN blocks when applied for Diffusion U-KAN.

Table 5: Ablation studies on using KAN layers against MLPs. The default setup is denoted.

KAN vs. MLP	IoU↑	F1↑	Gflops
KAN×3	65.26	78.75	14.02
MLP+KAN+KAN	64.12	77.86	14.29
KAN+MLP+KAN	63.82	77.58	14.29
KAN+KAN+MLP	64.30	77.95	14.29
MLP×3	63.49	77.07	14.84

Текущие результаты

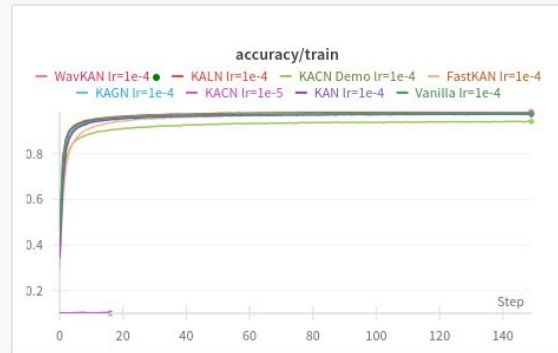
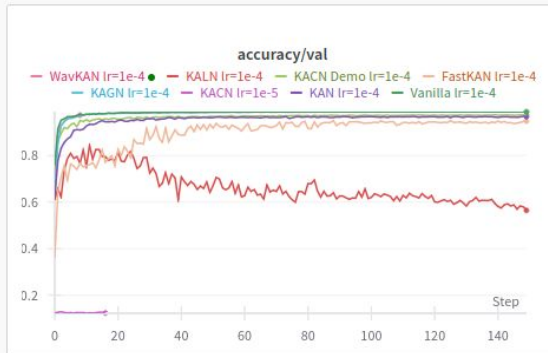
Search runs



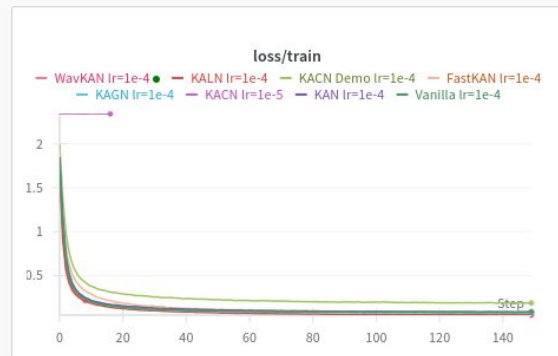
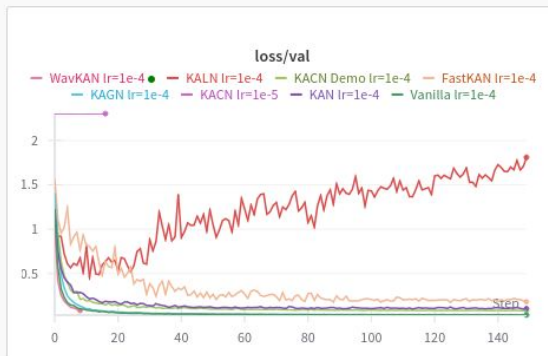
Name (8 visualized)

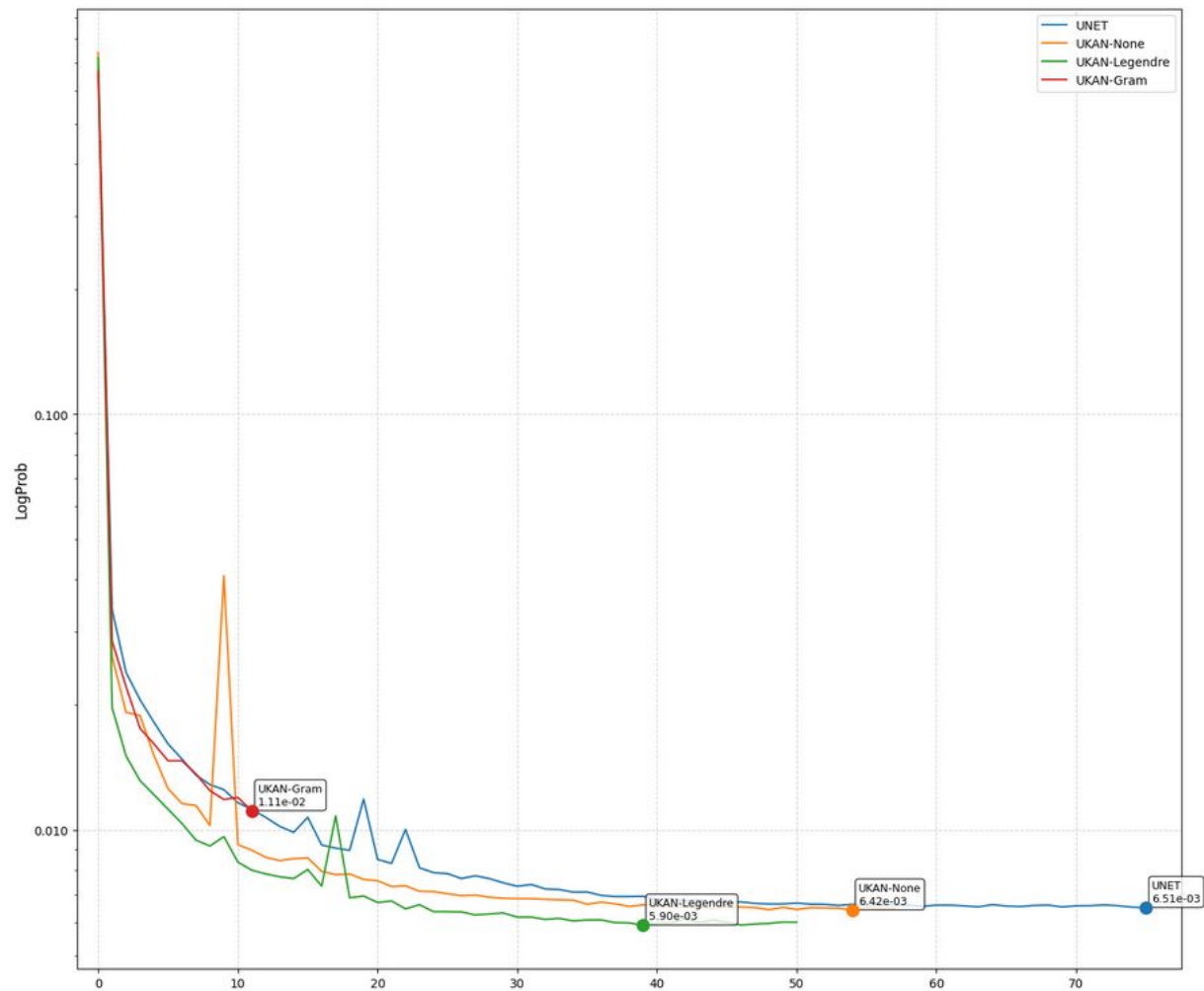
- WavKAN lr=1e-4
- KALN lr=1e-4
- KACN Demo lr=1e-4
- FastKAN lr=1e-4
- KAGN lr=1e-4
- KACN lr=1e-5
- KACN lr=1e-2
- KACN lr=1e-4
- KAN lr=1e-4
- Vanilla lr=1e-4

accuracy 2



loss 2





# Результаты

- 1) Имплементирован KAN с различными базисами
- 2) Сделаны эксперименты на датасетах MNIST, CIFAR, DIBCO
- 3) Улучшена UNET-архитектура для DIBCO



# Дальнейшее исследование

- 1) Исследование Conv KAN
- 2) Исследование Wavelet KAN
- 3) Квантование KAN